Geometry, Groups and Dynamics/GEAR Seminar (held at the Illinois hub of GEAR)

12:00 pm, Thursday, January 28, 2016, 243 Altgeld Hall

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Extending the \$\log (2k-1)\$-Theorem

Abstract: In this talk, I discuss current work that expands the scope of the \$\log (2k-1)\$-Theorem of Anderson, Canary, Culler and Shalen. This was a seminal result in that it articulated a relationship between a set of \$k\$ freely-generating isometries of hyperbolic 3-space and how they interacted with points in hyperbolic 3-space; namely, under certain conditions, at least one of the given isometries must move a point \$P\$ by a distance \$\ge \log(2k-1)\$. The result lay the foundation for future novel geometric-topological results. Here I discuss an expansion of the theorem, wherein we consider sets of length-\$n\$ words contained in a rank-2 free group \$\Xi\$ on 2 letters (one can consider \$\ge 2\$ letters via the same methods), and present a generalized version that restricts how these isometries displace points in hyperbolic 3-space. This has application to classifying certain hyperbolic 3-manifolds in that the volume of the resulting manifold \$M\$ gotten by quotient of hyperbolic 3-space with \$\Xi\$, is expected to have a bounded volume which is improved from known volume bounds. Video